

# Pattern Formation

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- What properties and processes are “easy” to obtain through physical dynamics alone?

# Reaction Diffusion Equations

$$\frac{\partial U}{\partial t} = D_V \nabla^2 U + F(U)$$

# Reaction Diffusion Equations

$$\frac{\partial U}{\partial t} = D_V \nabla^2 U + F(U)$$

$$\nabla^2 U = \frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2}$$

# Reaction Diffusion Equations

$$\frac{\partial U}{\partial t} = D_U \nabla^2 U + F(U, V)$$

$$\frac{\partial V}{\partial t} = D_V \nabla^2 V + G(U, V)$$

# Reaction Diffusion Equations



# Reaction Diffusion Equations



$$\frac{\partial U}{\partial t} = -UV^2 + F(1-U) + D_u \left( \frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} \right)$$

# Reaction Diffusion Equations



$$\frac{\partial U}{\partial t} = -UV^2 + F(1-U) + D_u \left( \frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} \right)$$

$$\frac{\partial V}{\partial t} = UV^2 - (F+k)V + D_v \left( \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} \right)$$

# Reaction Diffusion Equations

Find the simulation by Dirk Brockmann and Benjamin F. Maier  
that Chris uses here

<http://www.complexity-explorables.org/explorables/grayscott/>